## EFFECTS OF DYNAMIC FRICTION ON OBLIQUE IMPACT BEHAVIOR OF GOLF BALLS

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## **KEYWORDS**

Energy and friction in sport and leisure activities, oblique impact, golf ball, dynamic friction, sliding velocity, contact area

## ABSTRACT

A previous study [1] investigated oblique impacts of a golf ball of mass m (46 g) and radius r (21.3 mm) with a rigid target inclined at an angle  $\theta_i$  (30°) (Fig. 1a) and demonstrated the following: (i) the contact force N and area A rose in the early phases of the impact and then reduced in the later phases (Figs. 1b and c); and (ii) the angular velocity  $\omega$  can depend on A and the ball centre velocity  $u_b$ . However, the dynamic friction  $F_d$ causes the shear deformation of the ball, and consequently the discrepancy between  $u_b$  and the contact centre velocity  $u_c$ . This study used the analytical model proposed for the dynamic sliding friction on lubricated and non-lubricated inclines [2,3]. The contact area A and the velocity  $u_c$  were used to describe the dynamic friction force  $F_d = \lambda A u_c$ , where  $\lambda$  is a parameter related to the wear of the ball surface [4]. This study proposed an elastic sphere model to understand the mechanism of shear



Figure 1. Impact behaviour of a golf ball. a, The rotating and sliding motion of the ball at impact. b, The compression and shear deformation of the ball during impact. c, High-speed image of the ball hitting a transparent PMMA target at an impact velocity  $V_i = 32$  m s<sup>-1</sup>. The image was photographed from the reverse side of the target. d, High-speed images of the ball hitting a steel target at  $V_i = 37$  m s<sup>-1</sup>. Markings were made on the dimples to enable ball surface measurement.



Figure 2. Tangential ball centre velocity  $u_b$  and contact centre velocity  $u_c$  for  $V_i = 37$  m s<sup>-1</sup>.  $u_c$  reduced in the initial phases of the impact, rose in the intermediate phases, and then reduced again in the final phases, whereas  $u_b$  showed the opposite trend.

deformation during oblique impacts.

Figure 2 shows the tangential ball centre velocity  $u_b$  and contact centre velocity  $u_c$  versus time t, where the experimental results were indicated with symbols; those derived from the proposed analytical model are indicated using solid curves.  $u_c$  showed three phases of noticeable velocity reduction, rise, and reduction once again.  $u_b$  showed the opposite velocity changes. The analytical velocities  $u_b$  and  $u_c$  are shown in Fig. 2. Although the analysis yielded discrepancies from the experimental results, the model represented all of the important qualitative features of the velocity changes at the ball centre and contact centre.

## REFERENCES

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